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# Classification methods for documents with both fixed and free formats by PLSI model

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Abstract — Based on information retrieval model especially probabilistic latent semantic indexing (PLSI) model, we discuss methods for classification and clustering of a set of documents. A method for classification is presented and is demonstrated its good performance by applying to a set of benchmark documents with free format (text only). Then the classification method is modified to a clustering method and the clustering method is applied to partition experimental documents with fixed and free formats into two clusters, where the experimental documents are obtained from student questionnaires. Since the experimental documents are already categorized, the clustering method can be clearly evaluated its performance. The method has better performance compared to the conventional one based on the vector space model. The purpose of these questionnaires is to obtain useful knowledge for improvements in quality of education.

#### 1. Introduction

Recent development in information retrieval techniques enables us to process a large amount of text data. Based on the probabilistic latent semantic indexing (PLSI) model [Hoffman99], a new classification methods for documents, which are composed of both fixed and free formats, is proposed [HIASG04]. The documents with fixed format imply items such as those of selecting one from sentences, words, symbols, or numbers. While the documents with free format are the usual texts. We can find such documents in technical paper archives, questionnaires, or knowledge collaboration. In the case of paper archives, the documents with fixed format (called items in this paper) correspond to the name of authors, the name of journals, the year of publication, the name of publishers, the name of countries, and so on.

In this paper, as is found in the traditional vector space model of information retrieval systems, a co-occurrence matrix is used for the representation of a document set. The documents with fixed format are represented by an item-document matrix  $G=[g_{mj}]$ , where  $g_{mj}$  is the selected result of the item m  $(i_m)$  in the document j (d). The documents with free format are also represented by a term-document matrix  $H=[h_{ij}]$ , where  $h_{ij}$  is the frequency of the term i (i) in the document j (d). The dimensions of matrices G and H are  $I \times D$ , and  $I \times D$ , respectively. Both matrices are compressed into those with smaller dimensions by the probabilistic decomposition in PLSI [Hofmann99] similar to the single valued decomposition (SVD) in LSI (latent semantic indexing) [BYRN99]. The unobserved states are  $z_k$  (k=1,2,...,K). Introducing a weight  $\lambda$   $(0 \le \lambda \le 1)$ , the log-likelihood function corresponding to matrix  $[\lambda G^T, (1-\lambda)H^T]^T$  is maximized by the EM algorithm [CH01], where  $A^T$  is the transposed matrix of A. Then we obtain the probabilities  $Pr(z_k)$  (k=1,2,...,K), and the conditional probabilities  $Pr(l_i|z_k, l_m)$ , and  $Pr(d_i|z_k)$ . Using these probabilities,  $Pr(l_m, d)$  and  $Pr(l_n, d)$  are derived. We decide the state for  $d_i$  depending on  $Pr(z_k|d)$ , and a similarity function between  $z_k$  and  $z_k$  can be defined in the usual way, i.e., by cosine, or by inner product. By these preparations, we use the group average distance method with the similarity

measure for agglomeratively clustering the state  $z_k$  's until the number of clusters becomes S, where  $S \le K$  [HC03].

To show the effectiveness of the methods, first we apply them into a test document set which has been already categorized. Then as an experiment, we apply the proposed method into a document set given by student questionnaires [SIGIH03], where the students are the members of a class (Introduction to computer science, in the second academic year, undergraduate school) for one of the present authors. The contents of the questionnaires consist of questions answered with fixed format: e.g., Are you interested in wearable computers? (Its answer is yes or no), and questions, with free format: e.g., Write your image of computers. Merging the documents of students from two different classes, then the merged documents are classified into two categories. We show that each member of the partitioned classes coincides with that of the original classes at high rate. Its better performance is compared to the conventional method based on the vector space model. A final object of this experiment is to find helpful leads to the faculty development [HIASG04][IIGSH03-b].

#### 2. Information Retrieval Model

Early information retrieval systems adopted (1) Boolean model, and based on index terms (i.e., keywords) some of which are still in use for commercial purposes. To avoid over-simplification by this model, and to enable ranking the relevant document together with automatic indexing, (2) vector space (VS) model was proposed in early '70s [Salton71].

To improve the performance of the VS model, latent semantic indexing (LSI) model was studied by reducing the dimension of the vector space using single valued decomposition (SVD) [BYRN99].

As a similar approach, probabilistic latent semantic indexing (PLSI) model based on a statistical latent class model has recently been proposed by T. Hofmann [Hofmann99].

## 2.1 The Vector Space Model (VSM)

The VS model uses non-binary weights in the *i*-th (index) term ( $t_i$ ) in the *j*-th document ( $d_j$ ) for a given document set D and queries (q).

## [Vector Space Model]

Let T be a term set used for representing a document set D. Let  $t_i$  (i=1,2,...,T) be the i-th term in T, where T is a subset of the all term set  $T_0$  appeared in D, and  $d_j$  (j=1,2,...,D), the j-th document in D. Then a term-document matrix  $A=[a_{ij}]$  is given by the weight  $w_{ij} \geq 0$  associated with a pair  $(t_i, d_j)$ .

In the VS model, the weight  $w_{ij}$  is usually given by so-called the tf-idf value, where tf stands for the term frequency, and idf, the inverse document frequency. When the number of the i-th term  $(t_i)$  in the j-th document  $(d_j)$  is  $f_{i,j}$ , then  $tf(i,j) = f_{i,j}$ . When the number of documents in D for which the term  $t_i$  appears is df(i), then  $idf(i) = \log(D/df(i))$ . The tf-idf value is calculated by their product.

As the result, for the VS model the weight  $w_{ij}$  is given by

$$w_{ii} = tf(i,j) \cdot idf(i) \tag{1}$$

and is equal to  $a_{ij}$ .

The *i*-th row of the matrix A represents the frequency vector of the term  $t_i$  in D, and the *j*-th column, that of  $d_i$  in T, we use the term vector  $\mathbf{t}_i$  and the document vector  $\mathbf{d}_i$  as

$$t_i = (a_{i1}, a_{i2}, \dots, a_{iD})$$
 (2)

$$\boldsymbol{d}_{i} = (a_{1i}, a_{2i}, \dots, a_{Ti})^{\mathrm{T}} \tag{3}$$

where  $x^{T}$  is the transposed vector of x. Similar to the vector  $d_{j}$ , we also use a query vector q for a query q by the weight associated with the pair  $(t_{i}, q)$  as follows:

$$\boldsymbol{q} = (q_1, q_2, \dots, q_T)^{\mathrm{T}} \tag{4}$$

Then we can define the similarity  $s(q, d_i)$  between q and  $d_i$ . In the case of measuring it by cosine

of the angle between the vectors  $\mathbf{q}$  and  $\mathbf{d}_i$ , we have

$$s(q, d_j) = \frac{\boldsymbol{q}^{\mathrm{T}} \boldsymbol{d}_j}{|\boldsymbol{q}||\boldsymbol{d}_j|}$$
 (5)

#### 2.2 The Latent Semantic Indexing (LSI) Model

The LSI model is accomplished by mapping each document and query vector into a lower dimensional space by using SVD.

#### [Truncated LSI Model]

Let a term-document matrix  $A \in \mathbb{R}^{T \times D}$  be given by eq.(1). Then the matrix A is decomposed into  $A_K$  by the truncated SVD as follows:

$$A \to A_K = \begin{pmatrix} U_K & \hat{U} \begin{pmatrix} \Sigma_K & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} V_K^{\mathsf{T}} \\ \hat{V} \end{pmatrix}$$
$$= U_K \Sigma_K V_K^{\mathsf{T}}$$
 (6)

where

$$U_K \in \mathbb{R}^{D \times K}, \quad \Sigma_K \in \mathbb{R}^{K \times K}, \quad V_K \in \mathbb{R}^{T \times K}$$

and

$$K \le p \le \max\{T, D\}.$$

In eq.(6),  $|A-A_K|_F$  is minimized for any K, where p is the rank of A, and  $|\cdot|_F$  is the Frobenius matrix norm.

Let the term-document matrix A be given by the reduced rank matrix  $A_K$  by the truncated SVD, then a query vector  $\mathbf{q} \in \mathbb{R}^{T_{\times 1}}$  in eq.(4) is represented by  $\hat{\mathbf{q}} \in \mathbb{R}^{K_{\times 1}}$  in a space unit dimension K:

$$\hat{\boldsymbol{q}} = \Sigma_K^{-1} \boldsymbol{q} \in \mathbb{R}^{K \times 1} \tag{7}$$

<sup>1</sup>then  $s(q, d_i)$  is also computed by

 $<sup>^{1}</sup>$  In the other case,  $\, \hat{\pmb{q}} = \Sigma_{K}^{-1} U_{K}^{\mathrm{T}} \pmb{q} \in \pmb{\mathcal{R}}^{K \times 1}$ 

$$s(q, d_j) = \frac{\hat{\boldsymbol{q}}^{\mathrm{T}} \hat{\boldsymbol{d}}_j}{|\hat{\boldsymbol{q}}| |\hat{\boldsymbol{d}}_j|}$$
(8)

where

$$\hat{\boldsymbol{d}}_{i} = \Sigma_{K} V_{K}^{\mathrm{T}} \boldsymbol{e}_{i} \in \boldsymbol{R}^{K \times 1}$$

and

$$\mathbf{e}_{j} = (0, 0, \dots, 0, 1, 0, \dots, 0)$$
 (9)

is the *j*-th canonical vector.

#### 2.3 The Probabilistic Latent Semantic Indexing (PLSI) Model

In contrast to the LSI model, the PLSI model is based on mixture decomposition derived from a latent state model. A term-document matrix  $A=[a_{ij}]$  is directly given by term frequency  $tf(i,j)=f_{i,j}$ , i.e.,  $a_{ij}$  is the number of a term  $t_i$  in a document  $d_j$ .

In the LSI model, the matrix  $A \in \mathbb{R}^{T \times D}$  is decomposed into  $A_K$  with smaller dimension by SVD, using principal eigenvectors. While in the PLSI model, the matrix A is probabilistically decomposed into K unobserved states, where the k-th state is denoted by  $z_k \in Z$ , and Z, a set of states.

First, we assume both (i) an independence between pairs  $(t_i,d_j)$ , and (ii) a conditional independence between  $t_i$  and  $d_j$ , i.e., the term  $t_i$  and the document  $d_j$  are independent conditioned on the latent state  $z_k$ . A graphical representation is depicted in Fig. 1.

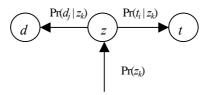


Figure 1: A graphical model for the PLSI model

The joint probability of  $t_i$  and  $d_j$ ,  $Pr(t_i, d_j)$  is given by

$$Pr(t_i, d_j) = \sum_{z_k \in \mathcal{Z}} Pr(d_j) Pr(t_i \mid z_k) Pr(z_k \mid d_j)$$
(10)

$$= \sum_{z_k \in Z} \Pr(z_k) \Pr(t_i \mid z_k) \Pr(d_j \mid z_k)$$
(11)

The number of the set of the states, or the cardinality of Z,  $\|Z\| = K$  satisfies

$$K \le \max\{T, D\} \tag{12}$$

## [PLSI Model]

Let a term-document matrix  $A=[a_{ij}]$  be given by only tf(i,j) of eq.(1). Then the probabilities  $Pr(d_i)$ ,  $Pr(t_i|z_k)$ , and  $Pr(z_k|d_i)$  are determined by the likelihood principle, i.e., by maximization of the following log-likelihood function:

$$L = \sum_{i,j} a_{ij} \log \Pr(t_i, d_j)$$
(13)

The maximization technique usually used for the likelihood function is the Expectation Maximization (EM) algorithm. The EM algorithm performs iteratively E-step and M-step as follows:

#### [EM algorithm]

According to eq.(11), the maximum value of eq.(13) is computed by alternating E-step and M-step until it converges.

E-step:

$$\Pr(z_{k} | t_{i}, d_{j}) = \frac{\Pr(z_{k}) \Pr(t_{i} | z_{k}) \Pr(d_{j} | z_{k})}{\sum_{k'} \Pr(z_{k'}) \Pr(t_{i} | z_{k'}) \Pr(d_{j} | z_{k'})}$$
(14)

M-step:

$$\Pr(t_i \mid z_k) = \frac{\sum_{j} a_{ij} \Pr(z_k \mid t_i, d_j)}{\sum_{i',j} a_{i'j} \Pr(z_k \mid t_{i'}, d_j)}$$
(15)

$$\Pr(d_{j} \mid z_{k}) = \frac{\sum_{i} a_{ij} \Pr(z_{k} \mid t_{i}, d_{j})}{\sum_{i, j'} a_{ij'} \Pr(z_{k} \mid t_{i}, d_{j'})}$$
(16)

$$Pr(z_k) = \frac{\sum_{ij} a_{ij} Pr(z_k \mid t_i, d_j)}{\sum_{i,j} a_{ij}}$$
(17)

Then we have the probabilities  $Pr(d_i)$ ,  $Pr(t_i | z_k)$ , and  $Pr(z_k | d_i)$ .

To avoid overtraining to the data in the EM algorithm, a temperature variable  $\beta$  ( $\beta$  > 0) is used, that is called a tempered EM (TEM) [Hofmann99]. At the E-step for the TEM, the numerator and the each term of the denominator of eq.(14) are replaced by those to the power of  $\beta$ .

## 3. Proposed Methods

We propose new classification and clustering methods based on the PLSI model. The methods are strongly dependent on the fact and property that the EM algorithm usually converges to the local optimum solution from starting with an initial value. Hence we use a representative document as the initial value for the EM algorithm. Since the latent states are regarded as concepts in the PLSI model, the state corresponds to the category or the cluster. Consequently, we can state that the methods presented in this paper have good performance for a document set with relatively small size.

#### 3.1 Classification method [IIGSH03-a]

Suppose a set of documents D for which the number of categories is K, where the K categories are denoted by  $C_1$ ,  $C_2$ , ...,  $C_K$ .

(1) Choose a subset of documents  $D^*$  ( $\subseteq D$ ) which are already categorized and compute representative document vectors  $d^*_1, d^*_2, ..., d^*_K$ :

$$\boldsymbol{d}_{k}^{*} = \frac{1}{n_{k}} \sum_{\boldsymbol{d}_{j} \in C_{k}} \boldsymbol{d}_{j} \tag{18}$$

where  $n_k$  is the number of selected documents to compute the representative document vector from  $C_k$ .

- (2) Compute the probabilities  $Pr(z_k)$ ,  $Pr(d_j | z_k)$  and  $Pr(t_i | z_k)$  which maximizes eq.(13) by the TEM algorithm, where |Z| = K.
- (3) Decide the state  $z_{\hat{k}} (= C_{\hat{k}})$  for  $d_j$  as

$$\max_{k} \Pr(z_k \mid d_j) = \Pr(z_{\hat{k}} \mid d_j) \Rightarrow d_j \in z_{\hat{k}}$$
(19)

By the algorithm described above, a set of documents is classified into K categories. If we can obtain the K representative documents prior to classification, they are used for  $d_k^*$  in eq.(18).

## 3.2 Clustering method [HC03][HIASG04]

Suppose a set of documents to be clustered into S clusters, where the S clusters are denoted by  $c_1, c_2, \ldots, c_S$ .

- (1) Choose a proper  $K \geq S$  and compute the probabilities  $\Pr(z_k)$ ,  $\Pr(d_j \mid z_k)$ , and  $\Pr(t_i \mid z_k)$  which maximizes eq.(13) by the TEM algorithm, where |Z| = K.
- (2) Decide the state  $z_{\hat{k}} (= c_{\hat{k}})$  for  $d_j$  as

$$\max_{k} \Pr(z_k \mid d_j) = \Pr(z_{\hat{k}} \mid d_j) \Rightarrow d_j \in z_{\hat{k}}$$
(20)

If S=K, then  $d_j \in C_{\hat{k}}$ .

(3) If  $S \le K$ , then compute a similarity measure  $s(z_k, z_k)$ :

$$S(z_k, z_{k'}) = \frac{z_k^{\mathrm{T}} z_{k'}}{|z_k| |z_{k'}|}$$
(21)

$$\boldsymbol{z}_{k} = (\Pr(t_{1} \mid \boldsymbol{z}_{k}), \Pr(t_{2} \mid \boldsymbol{z}_{k}), \cdots, \Pr(t_{T} \mid \boldsymbol{z}_{k}))^{\mathrm{T}}$$
(22)

and use the group average distance method with the similarity measure  $s(z_k, z_k)$  for agglomeratively clustering the states  $z_k$ 's until the number of clusters becomes S. Then we

have S clusters, and the members of each cluster are those of a cluster of states.

By the above algorithm, a set of documents is clustered into *S* clusters.

## **Experimental Results**

We first apply the classification method to the set of benchmark documents [Sakai99], and verify its effectiveness. We then apply the clustering method to the set of student questionnaires as real documents to be analyzed whose answers are written in both fixed and free formats. All documents applied in this paper are written in Japanese.

#### 4.1 Document sets

The document sets which we use as experimental data are shown in Table 1.

Table 1: Document sets

|     | contents   | format               | amount                   | categorize              |
|-----|--|----------------------|--------------------------|-------------------------|
| (a) | articles of Mainichi<br>news paper in '94<br>[Sakai99] | free<br>(texts only) | 101,058<br>(see Table 2) | yes<br>(9+1 categories) |
| (b) | questionnaire  | fixed and free       | 135+35                   | yes (2 categories)      |
| (c) | (see Table 3 in detail)                                | (see Table 3)        | 135                      | no                      |

Table 2: Selected categories of newspaper

| category | contents | # articles | # used for<br>training | # used for<br>test |
|----------|----------|------------|------------------------|--------------------|
| $C_1$    | business | 100        | 50                     | 50                 |
| $C_2$    | local    | 100        | 50                     | 50                 |
| $C_3$    | sports   | 100        | 50                     | 50                 |
| total    |          | 300        | 150                    | 150                |

Table 3: Contents of initial questionnaire

| Format | Number of questions            | Examples  |  |
|--------|--------------------------------|---|--|
| Fixed  | 7 major expertions?            | <ul><li>For how many years have you used computers?</li><li>Do you have a plan to study abroad?</li><li>Can you assemble a PC?</li></ul>                                  |  |
| (item) | 7 major questions <sup>2</sup> | <ul> <li>Can you assemble a PC?</li> <li>Do you have any license in information technology?</li> <li>Write 10 terms in information technology which you know4.</li> </ul> |  |
| Free   | 5 questione3                   | - Write about your knowledge and experience on computers.   |  |
| (text) | 5 questions <sup>3</sup>       | <ul> <li>What kind of job will you have after graduation?</li> <li>What do you imagine from the name of the subject?</li> </ul>   |  |

 $<sup>^2</sup>$  Each question has 4·21 minor questions.  $^3$  Each text is written within 250·300 Chinese and Japanese characters.

<sup>&</sup>lt;sup>4</sup> There is a possibility to improve the performance of the proposed method by elimination of these items.

Table 4: Object classes

| Name of subject                                | Course          | Number of students |
|--|-----------------|--------------------|
| Introduction to Computer Science (Class CS)    | Science course  | 135                |
| Introduction to Information Society (Class IS) | Literary course | 35                 |

(a) in Table 1 is a document set composed of 101,058 articles of Mainichi newspaper in '94, which is prepared for benchmark data in Japan [Sakai99]. The articles are categorized into 9 categories and the others dependent on their contents (edited location in newspaper) such as economics, business, sports, or local.

While (b) in Table 1 is actual data i.e., student questionnaires for which the present authors want to analyze for obtaining useful knowledge from the data in order to manage the classes. Effective clustering gives a proper class partition depending on students' interests, their levels, their experiences and so on.

## 4.2 Classification problem: (a)

#### 4.2.1 Experiments conditions of (a)

As shown in Table 2, we choose three categories. 100 articles are randomly chosen from each category. The half of them is used for training, and the rest of them, for test.

As baseline classification methods to be compared to the proposed method, the following conventional methods are evaluated, where we call the classification method by the VS model simply as the VS method, that by the LSI model as the LSI method, and that by the PLSI model as the PLSI method.

#### The VS method:

classified by the cosine similarity measure between the representative document vector and a given document vector in the VS model.

#### The LSI method:

the same as the VS method except that the term-document matrix  $[a_{ij}]$  is compressed by SVD in the LSI model, where K=81 which corresponds to the condition that the cumulative distribution rate=70[%].

#### PLSI method:

the same as VS the method except that the matrix  $[\Pr(d_j|z_k)]$  is compressed by the PLSI model, where K=10.

The proposed method uses K=3.

#### 4.2.2 Results of (a)

Table 5 for each method shows the classified number of articles  $n_{k\hat{k}}$  from category  $C_k$  to  $C_{\hat{k}}$ , hence the number of the diagonal element  $n_{k\hat{k}}$  implies that of correct classification. Table 6 indicates the classification error rate for each method.

Table 5: Classified number form  $C_k$  to  $C_{\hat{k}}$  for each method

| method          |            | to $C_k$ |       |       |
|-----------------|------------|----------|-------|-------|
| method          | from $C_k$ | $C_1$    | $C_2$ | $C_3$ |
|                 | $C_1$      | 17       | 4     | 29    |
| VS method       | $C_2$      | 8        | 38    | 4     |
|                 | $C_3$      | 15       | 4     | 31    |
|                 | $C_1$      | 16       | 6     | 28    |
| LSI method      | $C_2$      | 6        | 43    | 1     |
|                 | $C_3$      | 12       | 5     | 33    |
|                 | $C_1$      | 41       | 0     | 9     |
| PLSI method     | $C_2$      | 0        | 47    | 3     |
|                 | $C_3$      | 13       | 6     | 31    |
|                 | $C_1$      | 47       | 0     | 3     |
| Proposed method | $C_2$      | 0        | 50    | 0     |
|                 | $C_3$      | 4        | 2     | 44    |

Table 6: Classification error rate

| method          | classification error [%] |
|-----------------|--------------------------|
| VS method       | 42.7                     |
| LSI method      | 38.7                     |
| PLSI method     | 20.7                     |
| Proposed method | 6.0                      |

Classification process by the EM algorithm is shown in Fig. 2 for step 1, 4, and 4096. At step 1, almost all document vectors are located in the center of the triangle. Then they move to each

state  $z_k$  (k=1,2,3) depending on the probability  $\Pr(z_k | d_j)$  (k=1,2,3) at step L as L increases. Finally, each document vector is on the lines with satisfying  $\Pr(z_1 | d_j) + \Pr(z_2 | d_j) + \Pr(z_3 | d_j) = 1$ .

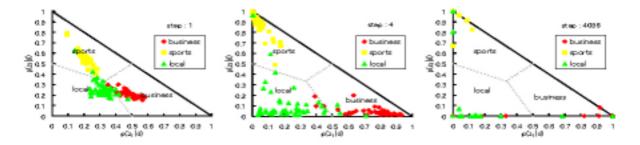


Figure 2: Classification process by EM algorithm

We see that the proposed classification method is clearly superior compared to the conventional methods.

## 4.3 Clustering problem: (b)

As stated above, we demonstrated the effectiveness of the proposed classification method. Based on this verification, we extend it to a clustering method.

We assume that characteristics of the students in Class CS are different from those in Class IS, because their majors are obviously distinct.

First, the documents of students in Class CS and those in Class IS are merged. Then the merged documents are partitioned into two clusters by the clustering method in 3.2, as shown in Fig. 3. We can expect that one cluster contains only the documents in Class CS and the other cluster, in Class IS. Since we know whether the document comes from Class CS or Class IS, the experiment is regarded as a classification problem, hence we can easily evaluate the performance of the clustering method by clustering error  $\Pr(\{k \neq \hat{k}\}) = C(e)$ .

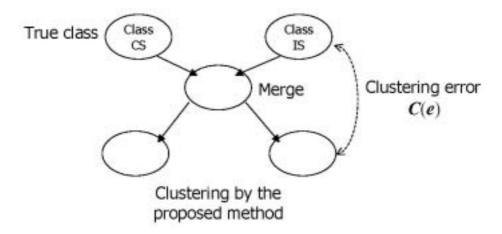


Figure 3: Class partition problem by clustering method

#### 4.3.1 Experiments condition of (b)

Substituting  $[\lambda G^{T}, (1-\lambda)H^{T}]^{T}$  into  $A=[a_{ij}]$  in eq.(13), the log-likelihood function L is computed [HC03].

This condition is added to the clustering method in 3.2 before step (1). Then documents given by student questionnaire in two classes, Class CS and Class IS are applied. As shown in Table 4, the total number of students is 170.

As another clustering method to be compared to that developed in this paper, the VS clustering method is evaluated, where the VS (clustering) method uses *tf-idf* value for matrix A in the VS model.

## 4.3.2 Results of (b)

Since S=2, clustering error occurs when  $d_j$  in Class CS is classified into Class IS, and vice versa. Fig. 4 shows the clustering error rate C(e) vs.  $\lambda$ , where  $\lambda$  is the weight for matrices G and H. If  $\lambda=0$ , then only the matrix H is used which implies the case of use of text (free format) only.

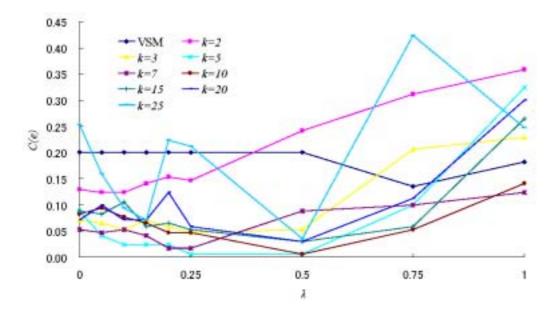


Figure 4: Clustering error vs.  $\lambda$ 

The result shows the superiority of the clustering method discussed in this paper. Choosing  $\lambda=0.5$  will be favorable to minimize the clustering error. We see that C(e) decreases as K increases.

If K becomes large, however, the performance will go down because of overfitting. Fig. 5 shows there is the optimum value of K to minimize C(e), although it is difficult to find it out. We also show clustering process for the EM algorithm at step 1, 4, and 1024 for K=2 and K=3 in Fig. 6. We see that the EM algorithm works well for clustering the document set.

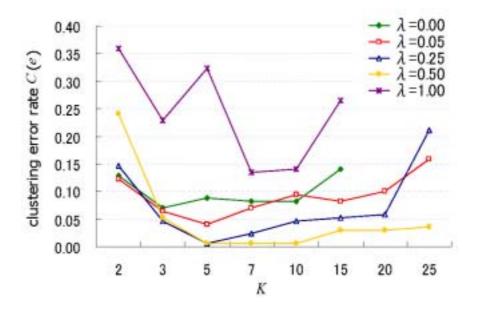


Figure 5: Clustering error rate C(e) vs. K

## K=2

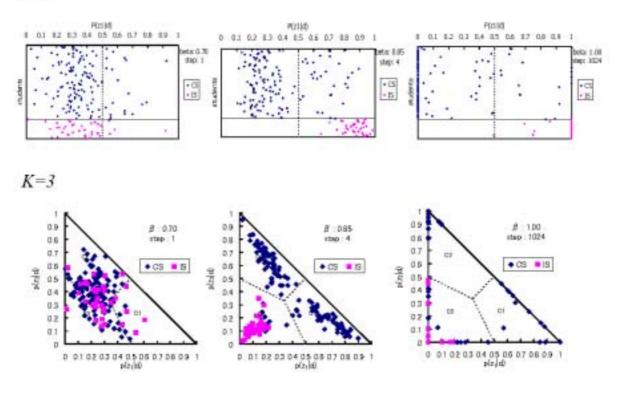


Figure 6: Clustering process by EM algorithm

## 5. Concluding Remarks

We have proposed a classification method for a set of documents and extend it to a clustering method. The classification method exhibits its better performance for a document set with comparatively small size by using the idea of the PLSI model.

The clustering method also has good performance. We show that it is applicable to documents with both fixed and free formats by introducing a weighting parameter  $\lambda$ .

In the case of clustering problem (b), we tried to apply the MDL principle [Rissanen83] to decide the optimum value of K. We see that the negative log-likelihood function, -L decreases slowly as K increases. While the penalty term,  $\frac{K}{2} \log D$  increases rapidly as K increases. If the number of the clusters S and that of the states K are small, then the optimum value of K will be small. This suggests us that there is a possibility to apply Bayesian probabilistic latent semantic

indexing (BPLSI) model [GITSH03][GIH03] into the clustering problems. Although the optimum value of the number of the states K is still hard to decide, the method is robust in choosing K for small K and S.

As an important related study, it is necessary to develop a method for abstracting the characteristics of each cluster [HIIGS03][IIGSH03-b]. An extension to a method for a set of documents with comparatively large size also remains as a further investigation.

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